Carnegie Mellon University

Database Query Optimization

Query Cost Models: Cardinality Estimation

ADMINISTRIVIA

Project #1 is due Friday Feb 28th.

Project #2 proposals are due Monday Mar 10th.

LAST CLASS

We discussed the data structures that DBMSs maintain to summarize the contents of tables.

→ Most Common: Equi-Depth, End-Bias Histograms (Heavy Hitters), HyperLogLog

Today's class is about how the optimizer's cost model uses these data structures...

CARDINALITY ESTIMATION

Cardinality estimation is the process of predicting the number of rows that will be returned by a query operation, such as a filter or join, to help the optimizer choose the most efficient execution plan.

The number of tuples that will be generated per operator is computed from its selectivity multiplied by the number of tuples in its input.

TODAY'S AGENDA

Cardinality Estimation Basics
The Germans' Survey
Implementations

CARDINALITY ESTIMATION

There are three cardinality estimations on logical expressions an optimizer must support as the core of its cost model:

- → Selection Conditions (filters)
- → Join Size Estimation
- → Distinct Value Estimation

These will serve as building blocks for more complex expressions:

- → Multiple Joins
- \rightarrow Group By

Source: <u>EQOP Book</u>

DERIVABLE STATISTICS

For each relation R, the DBMS maintains statistics to approximate the following information:

- $\rightarrow N_R$: Number of tuples in R.
- $\rightarrow V(A,R)$: Number of distinct values for attribute A.

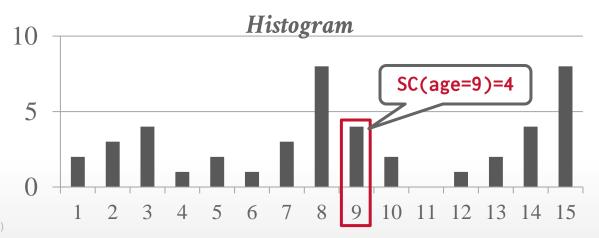
The <u>selection cardinality</u> SC(A,R) is the average number of records with a value for an attribute A given $N_R/V(A,R)$

The **selectivity** (**sel**) of a predicate **P** is the fraction of tuples that qualify.

SELECT * FROM people
WHERE age = 9

Equality Predicate: A=constant

- \rightarrow sel(A=constant) = #occurrences / |R|
- \rightarrow Example: sel(age=9) = 4/45 = 0.088

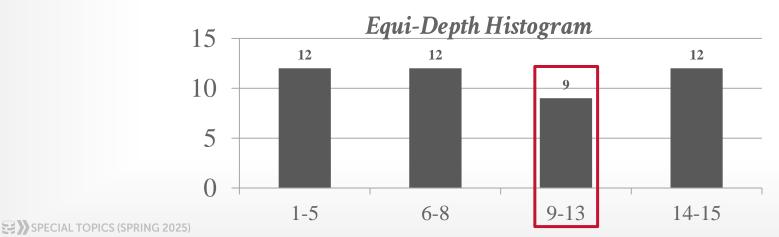


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SELECT * FROM people
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```

Equality Predicate: A=constant

- \rightarrow sel(A=constant) = #occurrences / |R|
- \rightarrow Example: $sel(age=9) = 4 \times 45 = 0.088$ $\approx (9/5)/45 \approx 1.8/45 \approx 0.04$



ASSUMPTIONS

Assumption #1: Uniform Data

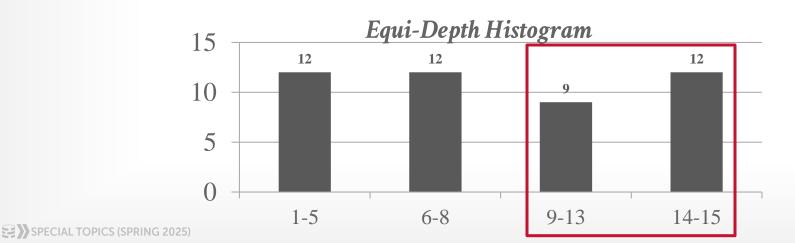
→ The distribution of values (except for the heavy hitters) is the same within a histogram bucket.

Range Predicate:

$$\rightarrow$$
 sel(A>= a) = (#RANGE-ROWS + #EQ-ROWS) / |R|

 \rightarrow Example: $sel(age >= 7) \approx ((9+12)$

SELECT * FROM people
WHERE age >= 7

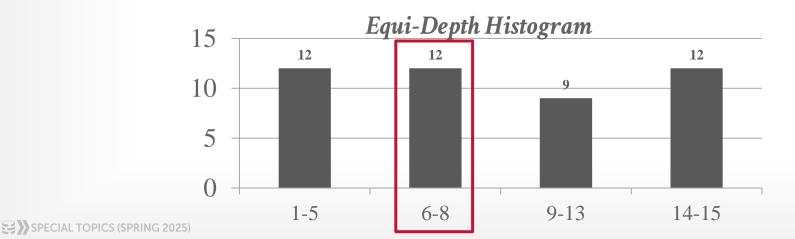


Range Predicate:

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 sel(A >= a) = (#RANGE-ROWS + #EQ-ROWS) / |R|

$$\rightarrow$$
 Example: $sel(age >= 7) \approx ((9+12) + (2 \times (12/3))) / 45$
 $\approx 29 / 45 \approx 0.6444$

SELECT * FROM people
WHERE age >= 7



Range Predicate:

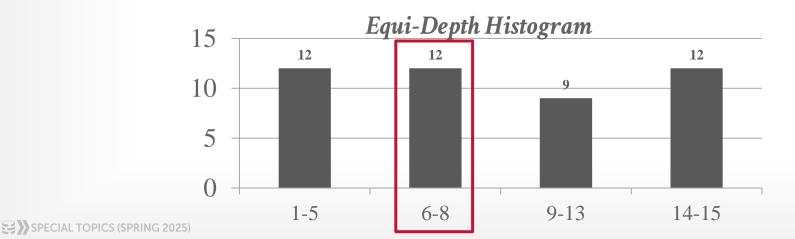
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 Example: $sel(age >= 7) \approx ((9+12) + (2 \times (12/3))) / 45$
 $\approx 29 / 45 \approx 0.6444$

SELECT * **FROM** people WHERE age >= 7



This assumes continuous distribution of values.



* FROM people

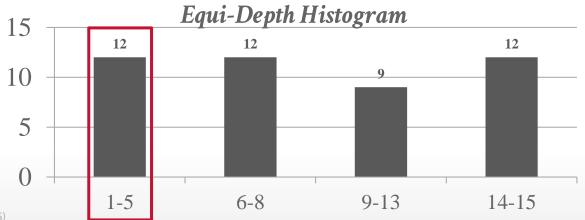
WHERE age !=

SINGLE SELECTION CONDITION

Negation Query:

- \rightarrow sel(not P) = 1 sel(P)
- → Example: $sel(age != 2) \approx 1 ((12/5)/45)$ $\approx 1 - (2.4/45) \approx 1 - 0.05 \approx 0.95$

⚠ Observation: Selectivity ≈ Probability



SPECIAL TOPICS (SPRING 2025)

We now can compute selectivities for individual predicates, but what happens if there are multiple predicates in a query?

→ Even though the predicates are on the same table, the attributes may have different distributions.

```
SELECT * FROM people
WHERE age = 2
AND name LIKE 'A%'
```

We now can compute selectivities for individual predicates, but what happens if there are multiple predicates in a query?

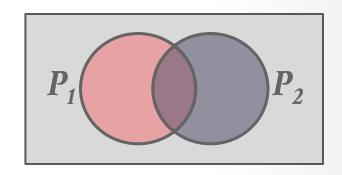
→ Even though the predicates are on the same table, the attributes may have different distributions.

Example:

```
\rightarrow sel(age = 2) \approx 0.053
```

 \rightarrow sel(name LIKE 'A%') \approx 0.1

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SELECT * FROM people
WHERE age = 2
AND name LIKE 'A%'
```



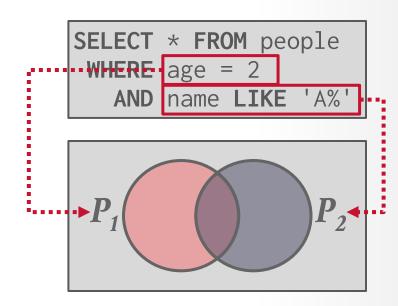
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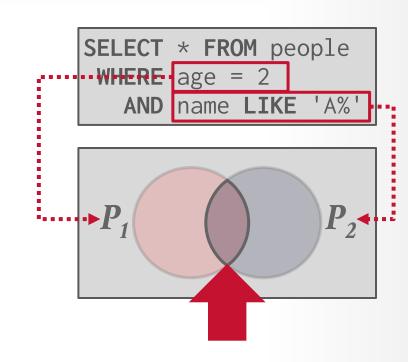


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- \rightarrow sel(age = 2) \approx 0.053
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ASSUMPTIONS

Assumption #1: Uniform Data

→ The distribution of values (except for the heavy hitters) is the same within a histogram bucket.

Assumption #2: Independent Predicates

→ The predicates on attributes are independent. The selectivity of the conjunction of two or more predicates is estimated as the product of their individual selectivities.

MULTIPLE SELECTION CONDITION

Conjunction:

```
 → sel(P1 \land P2) = sel(P1) \times sel(P2) 

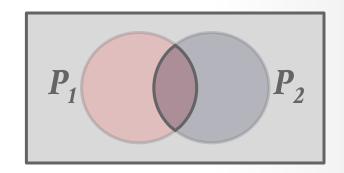
  → Example: sel(age=2 \land name LIKE'A%') 

  ≈ sel(age=2) × sel(name LIKE'A%') 

  ≈ 0.053 × 0.1 ≈ 0.0053
```

This assumes that the predicates are **independent**.

```
SELECT * FROM people
WHERE age = 2
AND name LIKE 'A%'
```

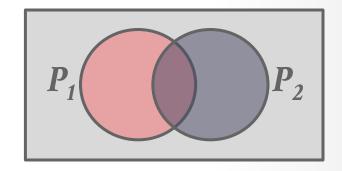


MULTIPLE SELECTION CONDITION

Disjunction:

```
\rightarrow sel(P1 \lor P2)
\approx sel(P1) + sel(P2) - sel(P1 \land P2)
\approx sel(P1) + sel(P2) - sel(P1) \times sel(P2)
```

```
SELECT * FROM people
WHERE age = 2
OR name LIKE 'A%'
```



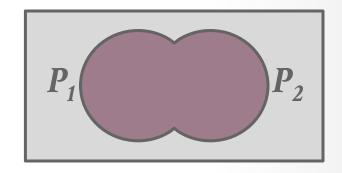
MULTIPLE SELECTION CONDITION

Disjunction:

```
 → sel(P1 \lor P2) 
 ≈ sel(P1) + sel(P2) - sel(P1 \land P2) 
 ≈ sel(P1) + sel(P2) - sel(P1) × sel(P2) 
 → Example: sel(age=2 \lor name LIKE 'A%') 
 ≈ 0.053 + 0.1 - (0.053 × 0.1) 
 ≈ 0.1477
```

This again assumes that the selectivities are **independent**.

```
SELECT * FROM people
WHERE age = 2
OR name LIKE 'A%'
```



CORRELATED ATTRIBUTES

Consider a database of automobiles:

```
\rightarrow # of Makes = 10, # of Models = 100
```

Then the following query shows up:

```
→ (make="Honda" AND model="Accord")
```

With the <u>independence</u> and <u>uniformity</u> assumptions, the selectivity is:

```
\rightarrow 1
/10 \times 1/100 \approx 0.001
```

But since only Honda makes Accords the real selectivity is 1/100 = 0.01

Source: Guy Lohman

JOIN SIZE ESTIMATION

Given a join of **R** and **S**, what is the range of possible result sizes in # of tuples?

→ In other words, for a given tuple of R, how many tuples of S will it match?

Assume each key in the inner relation will exist in the outer table.

ASSUMPTIONS

Assumption #1: Uniform Data

→ The distribution of values (except for the heavy hitters) is the same within a histogram bucket.

Assumption #2: Independent Predicates

→ The predicates on attributes are independent. The selectivity of the conjunction of two or more predicates is estimated as the product of their individual selectivities.

Assumption #3: Containment Principle

→ The domain of join keys overlap such that each key in the inner relation will also exist in the outer table.

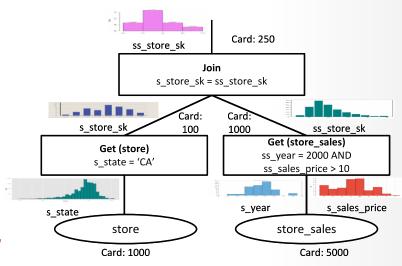
JOIN SIZE ESTIMATION

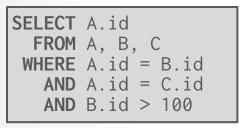
Align the buckets of the histograms so that their boundaries agree.

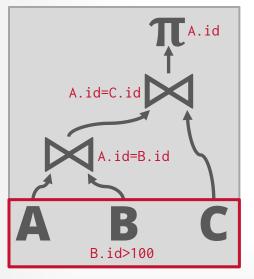
Compute a per bucket estimation of join size.

- \rightarrow Containment assumes that for each group g_R of tuples in R, it has a corresponding group g_S in S.
- \rightarrow Each tuple in g_R will match with tuples in g_S

Aggregate partial frequencies from joining each pair of buckets to get cardinality of the whole join.







Compute the cardinality of base tables

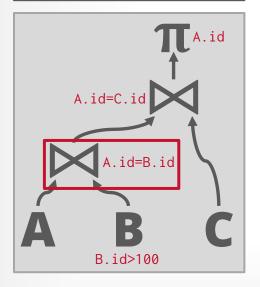
$$A \rightarrow |A|$$

$$R id > 100$$

$$B.id > 100 \rightarrow |B| \times sel(B.id > 100)$$

$$C \rightarrow |C|$$

SELECT A.id FROM A, B, C WHERE A.id = B.id AND A.id = C.id AND B.id > 100



Compute the cardinality of base tables

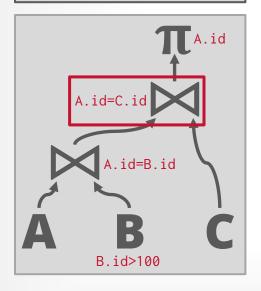
$$A \rightarrow |A|$$

 $B.id > 100 \rightarrow |B| \times sel(B.id > 100)$
 $C \rightarrow |C|$

Compute the cardinality of join results

$$A \bowtie B \approx (|A| \times |B|) / max(sel(A.id=B.id), sel(B.id>100))$$

```
SELECT A.id
FROM A, B, C
WHERE A.id = B.id
AND A.id = C.id
AND B.id > 100
```



Compute the cardinality of base tables

$$A \rightarrow |A|$$

 $B.id > 100 \rightarrow |B| \times sel(B.id > 100)$
 $C \rightarrow |C|$

Compute the cardinality of join results

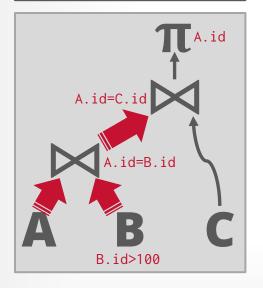
$$A \bowtie B \approx (|A| \times |B|) /$$

 $max(sel(A.id=B.id), sel(B.id>100))$

$$(A \bowtie B) \bowtie C \approx (|A| \times |B| \times |C|) /$$

 $max(sel(A.id=B.id), sel(B.id>100),$
 $sel(A.id=C.id))$

```
SELECT A.id
FROM A, B, C
WHERE A.id = B.id
AND A.id = C.id
AND B.id > 100
```



```
Compute the cardinality of base tables
  A \rightarrow |A| .....
  B.id > 100 \rightarrow |B| \times sel(B.id > 100)
  C \rightarrow |C|
Compute the cardinality of join results
  A\bowtie B \approx (|A| \times |B|)
             max(sel(A.id=B.id), sel(B.id>100)) \blacktriangleleft
  (A\bowtie B)\bowtie C \approx (|A|\times |B|\times |C|)
                      max(sel(A.id=B.id), sel(B.id>100),
                             sel(A.id=C.id)
```

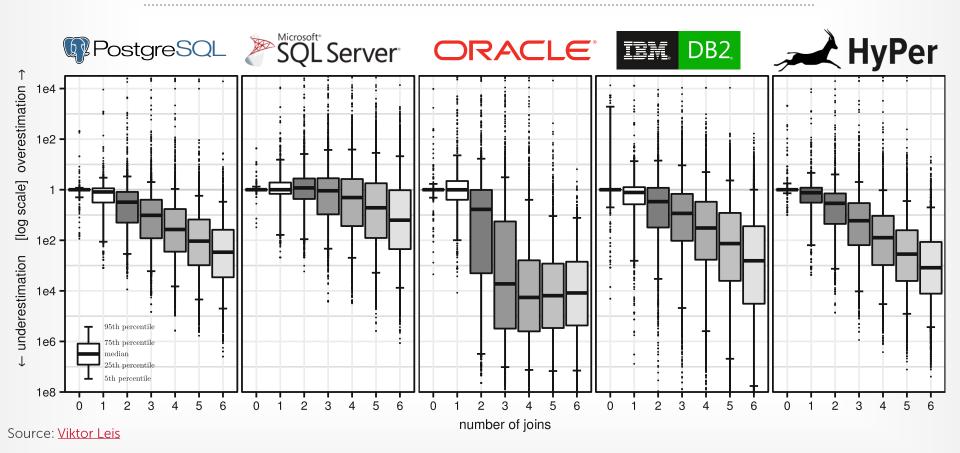
ESTIMATOR QUALITY

Evaluate the correctness of cardinality estimates generated by DBMS optimizers as the number of joins increases.

- → Let each DBMS perform its stats collection.
- → Extract measurements from query plan.

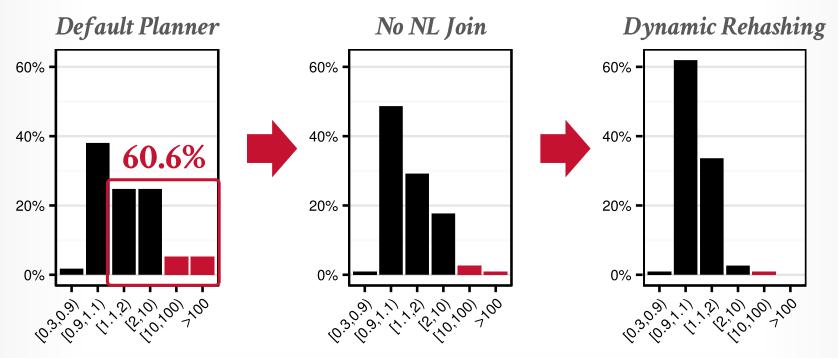
Compared five DBMSs using 100k queries from the JOB workload based on IMDB data.

ESTIMATOR QUALITY



EXECUTION SLOWDOWN

PostgreSQL v9.4 - JOB Workload



Slowdown compared to using true cardinalities

Source: Viktor Leis

LESSONS FROM THE GERMANS

Query opt is more important than a fast engine

→ Cost-based join ordering is necessary

Cardinality estimates are routinely wrong

 \rightarrow Try to use operators that do not rely on estimates

Hash joins + seq scans are a robust exec model

→ The more indexes that are available, the more brittle the plans become (but also faster on average)

Working on accurate models is a waste of time

→ Better to improve cardinality estimation instead

Source: Viktor Leis

IMPLEMENTATIONS

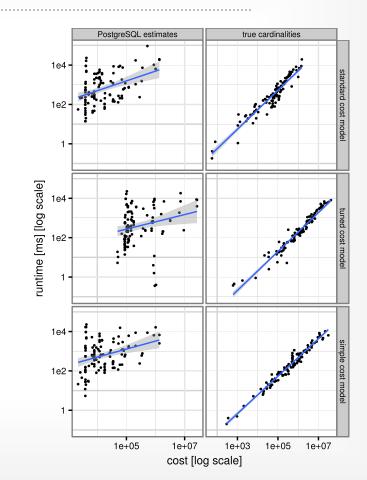
Postgres Microsoft SQL Server

POSTGRES COST MODEL

Cost of an operator is a weighted sum of the # of accessed disk pages and the amount of data processed in memory.

- → Distinguishes between sequential and random I/O.
- → Requires manual tuning the weights based on hardware characteristics.

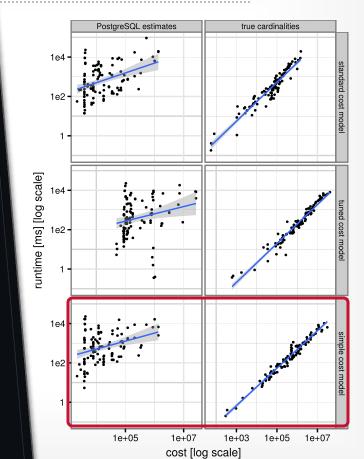
The Germans replaced Postgres' cost model with simple cost model to see what happens with query plans...

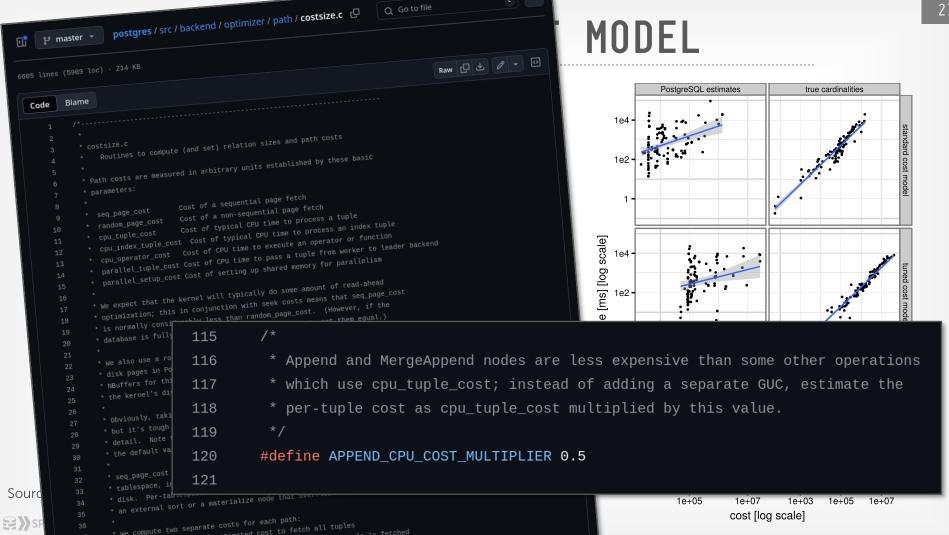


Source: Viktor Leis

imated cost to fetch all tuples

MODEL





SQL SERVER

Each operator's cost is based on producing all its output <u>and</u> the cost producing the first output.

→ Example: Nested-Loop Join vs. Index Nested-Loop Join

Maintains "row goals" to track the number of tuples are needed above in the query plan.

→ Example: Top-K / LIMIT clause

Combine predicates using an exponential backoff. Given a table R and predicate selectivities S_1 , S_2 , S_3 , ... S_n , where S_1 is the most selective and S_n the least:

Estimate =
$$|R| \times S_1 \times \sqrt{(S_2)} \times \sqrt{(\sqrt{(S_3)})} \times \sqrt{(\sqrt{(\sqrt{(S_4)})})} \dots$$

PARTING THOUGHTS

Cardinality estimation is the hardest part of building a query optimizer.

- → Lots of simplifying assumptions to make the problem more tractable.
- → But developers often don't revisit those assumptions...

Research suggests that accurate cardinality estimation is more important than sophisticated cost models.

All of this seems like it is the perfect usecase for machine learning...

THOUCHTS

PART. Peep this cardinality estimation work

Cardinality estimat a query optimizer.

- → Lots of simplifying tractable.
- \rightarrow But developers oft

Research suggests estimation is mor cost models.

All of this seems machine learning From: To:

Me

Date: 2/11/25 2:06 PM Spam Status: Spamassassin .

You're a huge pile shit and I am going to fuck you up when I see you again. I want my money back. Don't think you can roll up in Brooklyn like that again making big assumptions about how do we things in the streets.

Speaking of big assumptions, check out this hot piece of work:

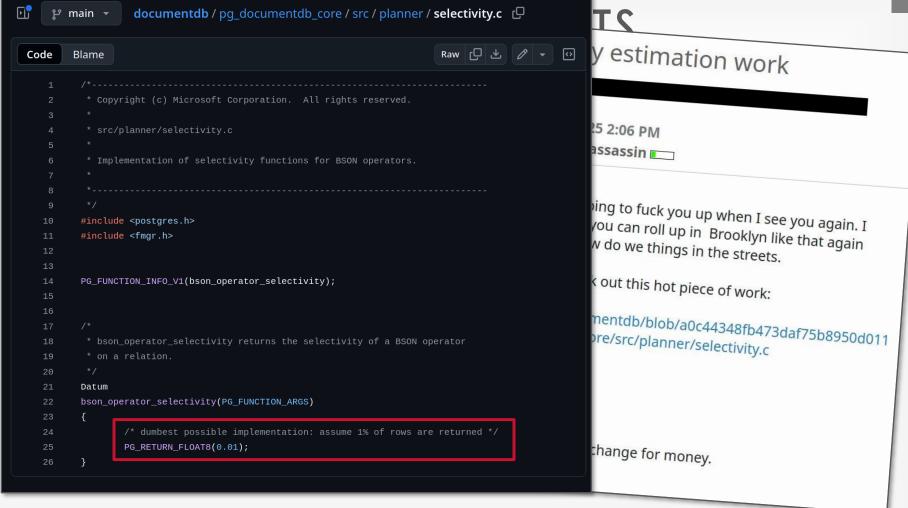
https://github.com/microsoft/documentdb/blob/a0c44348fb473daf75b8950d011 8201c0b3e6d19/pg_documentdb_core/src/planner/selectivity.c

Unmatched.

Erik Darling

https://erikdarling.com/

I'll make your SQL Server faster in exchange for money.



NEXT CLASS

Project #2 Proposals